## BEEE

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## Objectives

-Define basic components of electricity
-Recognize the 3 electrical classifications of materials
-Compare and contrast AC vs. DC
-Explain the concept of grounding
.Use Ohm' s law and Watt's law to express the relationship between current, voltage, and resistance

# Electricity can be broken down into: 

- Electric Charge
- Voltage
- Current
- Resistance


## Negative \& Positive Charges

- What do the effects of electricity in TV, radio, a battery, and lightening all have in common?
- Basic particles of electric charge with opposite polarities.


## Electrons

- The smallest amount of electrical charge having the quality called negative polarity.
- Electrons orbit the center of atoms.


## Protons

- The proton is a basic particle with positive polarity.
- Protons are located in the nucleus of atoms along with neutrons, particles which have neutral polarity.

Illustration of the Atomic Structures of Hydrogen and Helium Key: electrons (0), protons $\square$ ) and neutrons

| Copyright es 2001, Visionleaming, Fic. | Copyright © 2001, Visionleaming, Hic. |
| :---: | :---: |
| Hydrogen $\mathrm{z}=1 \text {, mass }=1$ | Helium $\mathrm{z}=2 \text {, mass }=4$ |

## Electrically, all materials fall into 1 of 3 classifications:

- Conductors
- Insulators
- Semi-Conductors


## Conductors

- Have 1 valence electron
- Materials in which electrons can move freely from atom to atom are called conductors.
- In general all metals are good conductors.
- The purpose of conductors is to allow electrical current to flow with minimum resistance.


## Insulators

- Have 8 valence electrons
- Materials in which electrons tend to stay put and do not flow easily from atom to atom are termed insulators.
- Insulators are used to prevent the flow of electricity.
- Insulating materials such as glass, rubber, or plastic are also called dielectrics, meaning they can store charges.
- Dielectric materials are used in components like capacitors which must store electric charges.


## Semi-Conductors

- Have 4 valence electrons
- Materials which are neither conductors nor insulators
- Common semi conductor materials are carbon, germanium and silicone.
- Used in components like transistors


## The Symbol for Charge

- The symbol for charge is Q which stands for quantity.
- The practical unit of charge is called the coulomb (C).
- One coulomb is equal to the amount of charge of $6.25 \times 10^{18}$ electrons or protons stored in a dielectric.


## Voltage

- Potential refers to the the possibility of doing work.
- Any charge has the potential to do the work of attracting a similar charge or repulsing an opposite charge.
- The symbol for potential difference is E (for electromotive force)
- The practical unit of potential difference is the volt (V)
- 1 volt is a measure of the amount of work required to move 1C of charge


## Current

- When a charge is forced to move because of a potential difference (voltage) current is produced.
- In conductors - free electrons can be forced to move with relative ease, since they require little work to be moved.
- So current is charge in motion.
- The more electrons in motion the greater the current.


## Amperes

- Current indicates the intensity of the electricity in motion. The symbol for current is I (for intensity) and is measured in amperes.
- The definition of current is: $\mathrm{I}=\mathrm{Q} / \mathrm{T}$
- Where $I$ is current in amperes, $Q$ is charge in coulombs, and T is time in seconds.


## 1 ampere = 1 coulomb per second



## Resistance

- Opposition to the flow of current is termed resistance.
- The fact that a wire can become hot from the flow of current is evidence of resistance.
- Conductors have very little resistance.
- Insulators have large amounts of resistance.


## Ohms

The practical unit of resistance is the ohm designated by the Greek letter omega: $\Omega$
A resistor is an electronic component designed specifically to provide resistance.

## Closed Circuits

- In applications requiring the use of current, electrical components are arranged in the form of a circuit.
- A circuit is defined as a path for current flow.


## Common Electronic Component Symbols

## 

$\}$
RESISTOR




## A Complex Audio Circuit



The vacuum tube predecessor to the classic 1176, this is the front-end of the Universal Audio 175-B ( version 175-C had a ratio switch like the 1176).

## Open Circuits

## An Open Circuit

Current can only exist where there is a conductive path (e.g. A length of wire). In the circuit shown in Figure 4-6, I
since there is no conductor between points $a \& b$. We referred to this is an open circuit.

Fig 4-6 $\begin{aligned} & \text { An open circuit has } \\ & \text { infinite resistance }\end{aligned}$

## The Circuit is a Load on the Voltage

## Source

- The circuit is where the energy of the source (battery) is carried by means of the current through the the various components.
- The battery is the source, since it provides the potential energy to be used.
- The circuit components are the load resistance they determines how much current the source will produce.


## Direction of Electron Flow

- The direction of electron flow in our circuit is from the negative side of the battery, through the load resistance, back to the positive side of the battery.
- Inside the battery, electrons move to the negative terminal due to chemical action, maintaining the potential across the leads.


## Electron Flow in a Simple Circuit



## DC

- Circuits that are powered by battery sources are termed direct current circuits.
- This is because the battery maintains the same polarity of output voltage. The plus and minus sides remain constant.


## Waveform of DC Voltage

$$
\underset{0}{\text { Voltage }} \frac{\prod_{D C}}{\text { Time } \longrightarrow}
$$

4.1a Steady Voltage

## Characteristics of DC

- It is the flow of charges in just one direction and...
- The fixed polarity of the applied voltage which are characteristics of DC circuits
- An alternating voltage source periodically alternates or reverses in polarity.
- The resulting current, therefore, periodically reverses in direction.
- The power outlet in your home is 60 cycle ac meaning the voltage polarity and current direction go through 60 cycles of reversal per second.
- All audio signals are AC also.


## Waveform of AC Voltage


4.1b Sinewave Voltage

## Complex Voltage



This is a more realistic view of what an audio signal's voltage would look like

## Comparison of DC \& AC

| DC Voltage | AC Voltage |
| :--- | :--- |
| Fixed polarity | Reverses polarity |
| Can be steady or vary in <br> magnitude | Varies in magnitude <br> between reversals in <br> polarity |
| Steady value cannot be <br> stepped up or down by a <br> transformer | Used for electrical power <br> distribution |
| Electrode voltage for tube <br> and transistor amps | l/O signal for tube and <br> transistor amps |
| Easier to measure | Easier to amplify |

Hoating Effects the same for both AC and DC current

## Many Circuits Include both AC \& DC Voltages

- DC circuits are usually simpler than AC circuits.
- However, the principles of DC circuits also apply to AC circuits.


## Impedance

- Impedance is resistance to current flow in AC circuits and its symbol is Z .
- Impedance is also measured in ohms.


## Grounding

- In the wiring of practical circuits one side of the voltage source is usually grounded for safety.
- For 120 V - ac power lines in homes this means one side of the voltage source is connected to a metal cold water pipe.
- For electronic equipment, the ground just indicates a metal chassis, which is used as a common return for connections to the source.


## Common Symbols/ Names for Ground in Electric Circuits



## Ohm' s Law

- The amount of current in a circuit is dependent on its resistance and the applied voltage. Specifically $I=E / R$
- If you know any two of the factors E, I, and R you can calculate the third.
- Current I = E/R
- Voltage E = IR
- Resistance R = E/I


## Current is Directly Proportional to Voltage for a Constant Resistance

## OHM's LAW



## Current is Inversely Proportional to Resistance for a Constant Voltage

## OHM's LAW



## Power

- The unit of electrical power is the watt.
- Power is how much work is done over time.
- One watt of power is equal to the work done in one second by one volt moving one coulomb of charge. Since one coulomb a second is an ampere:
- Power in watts = volts x amperes
- $P=E x$ I


## 3 Power Formulas

- $P=E \times I$
- $P=I^{2 \times R}$
- $P=E^{2} / R$


## Conversion Factors

| Prefix | Symbol | Relation to <br> basic unit | Examples |
| :--- | :--- | :--- | :--- |
| Mega | M | $1,000,000$ <br> or $1 \times 10^{6}$ | $5 \mathrm{M} \Omega=$ <br> $5 \times 10^{6} \Omega$ |
| Kilo | k | 1,000 or <br> $1 \times 10^{3}$ | $18 \mathrm{kV} \equiv$ <br> $18 \times 10^{3} \mathrm{~V}$ |
| Milli | m | .001 or <br> $1 \times 10^{-3}$ | $48 \mathrm{~mA} \equiv$ <br> $48 \times 10^{-3} \mathrm{~A}$ |
| Micro | $\mu$ | .000001 or <br> $1 \times 10^{-6}$ | $15 \mu \mathrm{~V} \equiv$ <br> $15 \times 10^{-6} \mathrm{~V}$ |



Presented By:
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## DEFINITION

- A physical agency caused by the motion of electrons, protons, and other charged particles, manifesting itself as an attraction, repulsion, magnetic, luminous, and heating effects, etc.


## ELEMENTS \& ATOMS

- Every known substance - solid, liquid or gas is composed of elements
- An atom is the smallest particle of an element that retains all the properties of that element
- Each element has it's own kind of atom


## ATOMS

- Inner part composed of protons \& neutrons

Outer part composed of electrons

- Protons = positive charge
- Neutrons = no charge

Electrons = negative charge

- Each element has a definite number of electrons ----and the same number of protons
- They are oppositely charged and therefore attract each other. This tends to hold the electrons in orbit around the atom.


## ELECTRICALLY BALANCED ATOM



ALUMINUM ATOM

## FREE ELECTRONS

- Some atoms are easily moved out of orbit
- The ability to move or flow is the basis of current electricity
- If channeled in a given direction, a flow of electrons occurs --- when flowed through a conductor it is dynamic electricity


## ELECTICAL MATERIALS

- CONDUCTOR - contains many free electrons --- gold, copper, silver, aluminum
- INSULATOR - contains few free electronsUsually non-metallic such as wood, rubber, glass, etc


## GENERATING ELECTRICITY

- Friction, pressure, heat, light, chemical reaction, and magnetism
- Magnetism is most practical \& inexpensive method
- Electricity is produced when a magnet is moved past a piece of wire, or wire is moved through a magnetic field


# VOLTAGE, CURRENT, \& RESISTANCE 

VOLTAGE - unit of measurement of electromotive force (EMF)

CURRENT - Continuous movement of electrons past a given point. (measured in amperes)

- RESISTANCE - Opposition to movement of electrons. Makes it possible to generate heat, contral current flow, \& supply correct voltage to devices


## OHM'S LAW

- George Simon Ohm
- Formulated a mathematical relationship between:
- Current
- Voltage
- Resistance
- Resistance = Impedance
- Resistance = DC
- Impedance = AC
- Interchangeable - Most Branch circuits


## DIRECT CURRENT

- Always flows in one direction
- Used to charge batteries, run some motors, operate magnetic lifting devices and welding equipment.


## ALTERNATING CURRRENT

- More common in electrical work

Changes rapidly in both direction and value

- Power companies produce power cheaper with alternating current


## ELECTRICAL HAZARDS

- SHOCK. Electric shock occurs when the human body becomes part of the path through which current flows.
- The direct result can be electrocution.
- The indirect result can be injury resulting from a fall or movement into machinery because of a shock


## ELECTRICAL HAZARDS

- BURNS. Burns can result when a person touches electrical wiring or equipment that is energized.
- ARC-BLAST. Arc-blasts occur from highamperage currents arcing through the air. This can be caused by accidental contact with energized components or equipment failure.


## Arc Flash and Arc Blasts

Arc Flash:
80\%-Burns due to ignition of clothing
Temperature35,000 F
Fatal Burns-10 ft. 2000 people hospitalized with burns
Molten metal

Arc Blast:
Pressure Wave Heat
Molten metal
Destruction of structures and life

## Arc Blast

Cause

- Short Circuit caused by working on energized equipment
- Dropped Tool
- Occurs in milliseconds
- Temp: 30,000 degrees
- Air expands very violently
- 15 tons of pressure


## ELECTRICAL HAZARDS

- ARC-BLAST. The three primary hazards associated with an arc-blast are:
- Thermal radiation.
- Pressure Wave.
- Projectiles.


## ELECTRICAL HAZARDS

- EXPLOSIONS. Explosions occur when electricity provides a source of ignition for an explosive mixture in the atmosphere.


## ELECTRICAL HAZARDS

- FIRES. Electricity is one of the most common causes of fires both in the home and in the workplace. Defective or misused electrical equipment is a major cause.


## EFFECTS ON THE HUMAN BODY

Depends on:
, Current and Voltage

- Resistance
- Path through body
- Duration of shock


## Effects of AC Electricity

- More than 3 mA- Painful shock- cause indirect accident
- More than 10 mA- Muscle contraction - "No Let Go" danger
- More than 30 mA - Lung paralysis, usually temporary


## Effects of AC Electricity

- More than 50 mA - Ventricular fibrillation, usually fatal
- 100 mA to 4 A-Certain ventricular fibrillation, fatal
- Over 4 A- Heart paralysis, severe burns


## Effects

- Protection
- Circuit Breakers
- Fuses
- 15 or 20 amps
- Property/equipment protection


## Conductors

- American Wire Gauge
- 12 gauge - 20 amps (Safely)
- 14 gauge - 15 amps
- 10 gauge - 30 amps
- What determines amount of amps through a circuit?
- How much the equipment draws
- How much "stuff" plugged in


## Protective Devices

- Fuses
- Circuit Breakers
- Trip or break circuit breakers if conductors exceed their ampacity


## Summary

- Current (I)
- Voltage (E or v)
- Resistance (R) (Ohms)


## Electrocution Triangle

- Electricity (levels)
- Time
- Path


## Wires

- Black $=$ hot $=$ Ungrounded Conductor
- White $=$ neutral $=$ Grounded Conductor (connected to grounding electrode/Grounding rod)


## Duplex Receptacle Correctly Wired to Designated Terminals



## How to check

- Wiring Checks
- Testers
- Different types


## Instruments

- Normal 3 light Tester
- Won't check resistance to ground
- Others - Check what the 3 light tester will
- Also checks resistance for ground


## Double Insulated

- Indicators
- No ground pin
- Plastic tool case
- Listed by NTL
- Marked as double insulated
- Square in a square
- Marked "double insulated"


## Grounding Conductors

- Equipment grounding conductor acts as a safeguard against insulation failure or faults in the other circuit conductors
- Not an energized conductor under normal conditions.
- Energized if a leak or fault in the normal current path
- Directs current back to the source
- Enabling fuses or circuit breakers to operate


## Identification of Conductors

- Grounded conductor i.d. and distinguished from other conductors w/ white or

w/ green, green w/ yellow stripes, or bare


## Polarity of connections

- Improper connection of these conductors ('hot and neutral') is most prevalent on smaller branch circuits:
- Standard 120 volt receptacle outlets
- Cord-and plug-connected equipment



## Reversed Polarity

- Reversed polarity is a condition when the grounded conductor
(neutral) is incorrectly connected to the ungrounded (hot) terminal of a plug, receptacle, or other type of conductor

Normal Wiring


### 1910.304(a)(2) Reverse Polarity



## Grounding

There are two kinds of grounding:

- 1. Electrical circuit or system grounding
$\circ$ 2. Electrical equipment grounding


## Electrical System Grounding

- One conductor of the circuit is intentior grounded to earth
- Protects circuit from lightning, or other tight voltage contact


## Equipment Grounding

- All metal frames \& enclosures of equipment are grounded by a permanent connection or bond
- The equipment gr

provides a path for dangerous fault current to return to the system ground at the supply source should a fault occur


## Grounding Equipment Connected by Cord and Plug

- Exposed non-current carrying metal parts of cord and plug connected equipment which may become energized shall be grounded
- If in a hazardous location
- If operated at over 150 volts





## CORD-AND PLUG-CONNECTED EQUIPMENT WITH A GROUNDING CONDUCTOR

Note that properly bonded conduit and associated metal enclosures can also serve as a grounding conductor.

## Ground fault circuit interrupters (GFCI’s)

- A GFCI is not an overcurrent device like a fuse or circuit breaker
- GFCI's are designed to sense an imbalance in current flow over the normal path


# Ground fault circuit interrupters (GFCI’s) 

- GFCI contains a special sensor that monitors the strength of the magnetic field around each wire in the circuit when current is flowing
- The field is proportional to the amount of current flow



## Ground fault circuit interrupters (GFCI's)

- If the current flowing in the black (ungrounded) wire is within 5 milliampers of the current flowing in the white (grounded) all the current will flow in the normal path
- If the current flow differs by more than $5 \mathrm{~mA}+/-1 \mathrm{~mA}$, the GFCI will quickly open the circuit



## HOW THE GFCI PROTECTS PEDPLE

(B' OPENING THE GIRGLIT WHEN CURRENT FLOWS THROUGH A GROUND-FAULT PATH)

## Testing GFCI's

- GFCl's are complex mechanisms, they must be tested on a regular basis
- Installation must be correct according to the listing \& labeling requirements or the GFCI will not protect as designed
- For permanently mounted types, once a month testing is recommended
- Portable GFCI's should be tested before each use! GFCl's have a test-circuit which imposes an artificial ground-foult when the test button is pushed


## Conductors Entering Boxes, Cabinets or Fittings

- All pull boxes, junction boxes and fittings must be provided with approved covers
- If covers are metal they must be grounded.
- Each outlet box must have a cover, faceplate or fixture canopy



## Judgment of application

- There are usually citations when the usage is obviously not temporary; and,
- When the cord is extended to some distant outlet in order to avoid providing a fixed outlet where needed


## Identification, Splices and Terminations

- Flexible cords shall only be used in continuous lengths, no taps or splices


Damaged cord improperly repaired

## Identification, Splices and Terminations

- Flexible cords shall be connected to devices and fittings so that strain relief is provided which will prevent pull from being directly transmitted to joints or terminal screws



## Footnote to Table S-4

(1) Workers in these groups do not need to be trained if their work or the work of those they supervise does not bring them or their employees close enough to exposed parts of electric circuits operating at 50 volts or more to ground for a hazard to exist.

## Should det be...



## Induction Motors



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## Introduction

- Three-phase induction motors are the most common and frequently encountered machines in industry
- simple design, rugged, low-price, easy maintenance
- wide range of power ratings: fractional horsepower to 10 MW
- run essentially as constant speed from zero to full load
- speed is power source frequency dependent
- not easy to have variable speed control
- requires a variable-frequency power-electronic drive for optimal speed control


## Construction

- An induction motor has two main parts
- a stationary stator
- consisting of a steel frame that supports a hollow, cylindrical core
- core, constructed from stacked laminations (why?), having a number -rorer roviding the space for the sta



## Construction

- a revolving rotor
- composed of punched laminations, stacked to create a series of rotor slots, providing space for the rotor winding
- one of two types of rotor windings
- conventional 3-phase windings made of insulated wire (wound-rotor) »similar to the winding on the stator
- aluminum bus bars shorted together at the ends by two aluminum rings, forming a squirrel-cage shaped circuit (squirrel-cage)
- Two basic design types depending on the rotor design
- squirrel-cage
- wound-rotor


## Construction



Squirrel cage rotor

Notice the
slip rings


## Construction



## Rotating Magnetic Field

- Balanced three phase windings, i.e. mechanically displaced 120 degrees form each other, fed by balanced three phase source
- A rotating magnetic field with constant magnitude is produced, rotating with a speed

$$
m_{\text {syme }}=\frac{120 f_{e}}{P} \quad \text { rpm }
$$

Where $f_{e}$ is the supply frequency and
 $P$ is the no. of poles and $n_{\text {sync }}$ is called the synchronous speed in rpm (revolutions per minute)

Rotating Magnetic Field

## Principle of operation

- This rotating magnetic field cuts the rotor windings and produces an induced voltage in the rotor windings
- Due to the fact that the rotor windings are short circuited, for both squirrel cage and wound-rotor, and induced current flows in the rotor windings
- The rotor current produces another magnetic field
- A torque is produced as a result of the interaction of those two magnetic fields

Where $\tau_{\text {ind }}$ is the induced torgue and $B_{R}$ and $B_{S}$ are the magnetic flux densfties $\overline{5}$ dfter botor and the stator respectively

## Induction motor speed

- At what speed will the IM run?
- Can the IM run at the synchronous speed, why?
- If rotor runs at the synchronous speed, which is the same speed of the rotating magnetic field, then the rotor will appear stationary to the rotating magnetic field and the rotating magnetic field will not cut the rotor. So, no induced current will flow in the rotor and no rotor magnetic flux will be produced so no torque is generated and the rotor speed will fall below the synchronous speed
- When the speed falls, the rotating magnetic field will cut the rotor windings and a torque is produced


## Induction motor speed

- So, the IM will always run at a speed lower than the synchronous speed
- The difference between the motor speed and the synchronous speed is called the Slip

$$
n_{\text {slip }}=n_{\text {sync }}-n_{m}
$$

Where $n_{\text {slip }}=$ slip speed
$n_{\text {sync }}=$ speed of the magnetic field
$n_{m}=$ mechanical shaft speed of the motor

## The Slip

Where $s$ is the slip

$$
S=\frac{n_{\text {synce }}-n_{m}}{n_{\text {synce }}}
$$

Notice that : if the rotor runs at synchronous speed

$$
s=0
$$

if the rotor is stationary

$$
s=1
$$

Slip may be expressed as a percentage by multiplying the above eq by 100, notice that the slip is a ratio and doesn't have units

## Example 7-1 (pp.387-388)

A 208-V, 10 hp , four pole, $60 \mathrm{~Hz}, \mathrm{Y}$ connected induction motor has a full-load slip of 5 percent

1. What is the synchronous speed of this motor?
2. What is the rotor speed of this motor at rated load?
3. What is the rotor frequency of this motor at rated load?
4. What is the shaft torque of this motor at rated load?

## Solution

1. $n_{\text {sync }}=\frac{120 f_{e}}{P}=\frac{120(60)}{4}=1800 \mathrm{rpm}$
2. 

$$
\begin{aligned}
n_{m} & =(1-s) n_{s} \\
& =(1-0.05) \times 1800=1710 \mathrm{rpm}
\end{aligned}
$$

3. 

$$
f_{r}=s f_{e}=0.05 \times 60=3 \mathrm{~Hz}
$$

4. 

$$
\begin{aligned}
\tau_{\text {load }} & =\frac{P_{\text {out }}}{\omega_{m}}=\frac{P_{\text {out }}}{2 \pi \frac{n_{m}}{60}} \\
& =\frac{10 \mathrm{hp} \times 746 \mathrm{watt} / \mathrm{hp}}{1710 \times 2 \pi \times(1 / 60)}=41.7 \mathrm{~N} . \mathrm{m}
\end{aligned}
$$

## Problem 7-2 (p.468)

A $220-\mathrm{V}$, three-phase, two-pole, $50-\mathrm{Hz}$ induction motor is running at a slip of 5 percent. Find:
(a) The speed of the magnetic fields in revolutions per minute
(b) The speed of the rotor in revolutions per minute
(c) The slip speed of the rotor
(d) The rotor frequency in hertz

## Solution

(a) The speed of the magnetic fields is

$$
n_{\mathrm{gyx}}=\frac{120 f_{e}}{P}=\frac{120(50 \mathrm{~Hz})}{2}=3000 \mathrm{r} / \mathrm{min}
$$

(b) The speed of the rotor is

$$
n_{\mathrm{sm}}=(1-s) n_{\mathrm{gypc}}=(1-0.05)(3000 \mathrm{r} / \mathrm{min})=2850 \mathrm{r} / \mathrm{min}
$$

(c) The slip speed of the rotor is

$$
n_{\text {dip }}=s n_{\text {sync }}=(0.05)(3000 \mathrm{r} / \mathrm{min})=150 \mathrm{r} / \mathrm{min}
$$

(d) The rotor frequency is

$$
f_{r}=\frac{n_{\text {slip }} P}{120}=\frac{(150 \mathrm{r} / \mathrm{min})(2)}{120}=2.5 \mathrm{~Hz}
$$

## Equivalent Circuit



## Power losses in Induction machines

Copper losses

- Copper loss in the stator $\left(P_{S C L}\right)=I_{I}^{2} R_{I}$
- Copper loss in the rotor $\left(P_{R C L}\right)=I_{2}^{2} R_{2}$
- Core loss ( $P_{\text {core }}$ )
- Mechanical power loss due to friction and windage
- How this power flow in the motor?


## Power flow in induction motor

$$
P_{\mathrm{in}}=\sqrt{3} V_{T} I_{L} \cos \theta
$$



## Power relations

$$
\begin{aligned}
& P_{i n}=\sqrt{3} V_{L} I_{L} \cos \theta=3 V_{p h} I_{p h} \cos \theta \\
& P_{S C L}=3 I_{1}^{2} R_{1} \\
& P_{A G}=P_{i n}-\left(P_{S C L}+P_{\text {core }}\right) \\
& P_{R C L}=3 I_{2}^{2} R_{2} \\
& P_{\text {conv }}=P_{A G}-P_{R C L} \\
& P_{\text {out }}=P_{\text {conv }}-\left(P_{f+w}+P_{\text {stray }}\right)
\end{aligned}
$$

## Equivalent Circuit

- We can rearrange the equivalent circuit as



## Power relations

$$
\begin{aligned}
& P_{i n}=\sqrt{3} V_{L} I_{L} \cos \theta=3 V_{p h} I_{p h} \cos \theta \\
& P_{S C L}=3 I_{1}^{2} R_{1} \\
& P_{A G}=P_{i n}-\left(P_{S C L}+P_{\text {core }}\right)=P_{c o n v}+P_{R C L}=3 I_{2}^{2} \frac{R_{2}}{s}=\frac{P_{R C L}}{s} \\
& P_{R C L}=3 I_{2}^{2} R_{2} \\
& P_{\text {conv }}=P_{A G}-P_{R C L}=3 I_{2}^{2} \frac{R_{2}(1-s)}{s}=\frac{P_{R C L}(1-s)}{s} \\
& P_{\text {out }}=P_{\text {conv }}-\left(P_{f+w}+P_{\text {stray }}\right)
\end{aligned}
$$

## Torque, power and Thevenin's Theorem

- Thevenin's theorem can be used to transform the network to the left of points 'a' and 'b' into an equivalent voltage source $V_{1 e q}$ in series with equivalent impedance $R_{e q}+j X_{e q}$



## Torque, power and Thevenin's Theorem



$$
\begin{aligned}
& V_{\text {leq }}=V_{1} \frac{j X_{M}}{R_{1}+j\left(X_{1}+X_{M}\right)} \\
& R_{e q}+j X_{e q}=\left(R_{1}+j X_{1}\right) / / j X_{M}
\end{aligned}
$$

## Torque, power and Thevenin's Theorem

$$
I_{2}=\frac{V_{\text {leq }}}{Z_{T}}=\frac{V_{\text {leq }}}{\sqrt{\left(R_{e q}+\frac{R_{2}}{s}\right)^{2}+\left(X_{e q}+X_{2}\right)^{2}}}
$$

Then the power converted to mechanical ( $P_{\text {conv }}$ )

$$
P_{c o n v}=I_{2}^{2} \frac{R_{2}(1-s)}{s}
$$

And the internal mechanical torque ( $T_{\text {conv }}$ )

$$
T_{c o n v}=\frac{P_{\text {conv }}}{\omega_{m}}=\frac{P_{\text {conv }}}{(1-s) \omega_{s}}=\frac{I_{2}^{2} \frac{R_{2}}{s}}{\omega_{s}}
$$

## Torque, power and Thevenin's Theorem

$$
T_{\text {conv }}=\frac{1}{\omega_{s}}\left(\frac{V_{\text {leq }}}{\sqrt{\left(R_{e q}+\frac{R_{2}}{s}\right)^{2}+\left(X_{e q}+X_{2}\right)^{2}}}\right)^{2}\left(\frac{R_{2}}{s}\right)
$$

$$
T_{\text {comn }}=\frac{1}{\omega_{s}} \frac{V_{\text {leq }}^{2}\left(\frac{R_{2}}{s}\right)}{\left(R_{\text {eq }}+\frac{R_{2}}{s}\right)^{2}+\left(X_{\text {eq }}+X_{2}\right)^{2}}
$$

## Torque-speed characteristics



Typical torque-speed characteristics of induction motor

## Maximum torque

- Maximum torque occurs when the power transferred to $R_{2} / s$ is maximum.
- This condition occurs when $R_{2} / s$ equals the magnitude of the impedance $R_{e q}+j\left(X_{e q}+X_{2}\right)$

$$
\frac{R_{2}}{s_{T_{\max }}}=\sqrt{R_{e q}^{2}+\left(X_{e q}+X_{2}\right)^{2}}
$$

$$
s_{T_{\max }} \equiv \frac{R_{2}}{\sqrt{R_{e_{q}}^{2}+\left(X_{\text {eq }}+X_{2}\right)^{2}}}
$$

## Maximum torque

- The corresponding maximum torque of an induction motor equals

$$
T_{\max }=\frac{1}{2 \omega_{o_{s}}}\left(\frac{V_{e e_{I}}^{2}}{R_{e_{e_{I}}}+\sqrt{R_{e_{q_{I}}}^{2}+\left(X_{e e_{I}}+X_{2}\right)^{2}}}\right)
$$

- The slip at maximum torque is directly proportional to the rotor resistance $R_{2}$
- The maximum torque is independent of $R_{2}$


## Maximum torque

- Rotor resistance can be increased by inserting external resistance in the rotor of a woundrotor induction motor.
- The value of the maximum torque remains unaffected but the speed at which it occurs can be controlled.


## Maximum torque



Effect of rotor resistance on torque-speed characteristic

## Problem 7-5 (p.468)

A $50-\mathrm{kW}, 440-\mathrm{V}, 50-\mathrm{Hz}$, six-pole induction motor has a slip of 6 percent when operating at full-load conditions. At full-load conditions, the friction and windage losses are 300 W , and the core losses are 600 W. Find the following values for full-load conditions:
(a) The shaft speed $n_{m}$
(b) The output power in watts
(c) The load torque $\tau_{\text {ladd }}$ in newton-meters
(d) The induced torque $\tau_{\text {ind }}$ in newton-meters
(e) The rotor frequency in hertz

## Solution to Problem 7-5 (p.468)

(a) The synchronous speed of this machine is

$$
n_{\mathrm{gync}}=\frac{120 f_{e}}{P}=\frac{120(50 \mathrm{~Hz})}{6}=1000 \mathrm{r} / \mathrm{min}
$$

Therefore, the shaft speed is

$$
n_{m}=(1-s) n_{\text {gyx }}=(1-0.06)(1000 \mathrm{r} / \mathrm{min})=940 \mathrm{r} / \mathrm{min}
$$

(b) The output power in watts is 50 kW (stated in the problem).
(c) The load torque is

$$
\tau_{\text {load }}=\frac{P_{\mathrm{OUT}}}{\omega_{\mathrm{m}}}=\frac{50 \mathrm{~kW}}{(940 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \frac{1 \mathrm{~min}}{60 \mathrm{~s}}}=508 \mathrm{~N} \cdot \mathrm{~m}
$$

(d) The induced torque can be found as follows:

$$
\begin{aligned}
& P_{\text {caxv }}=P_{\text {out }}+P_{\text {Few }}+P_{\text {cese }}+P_{\text {mice }}=50 \mathrm{~kW}+300 \mathrm{~W}+600 \mathrm{~W}+0 \mathrm{~W}=50.9 \mathrm{~kW} \\
& \tau_{\text {ind }}=\frac{P_{\text {carv }}}{\omega_{\mathrm{m}}}=\frac{50.9 \mathrm{~kW}}{(940 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \frac{1 \mathrm{~min}}{60 \mathrm{~s}}}=517 \mathrm{~N} \cdot \mathrm{~m}
\end{aligned}
$$

(e) The rotor frequency is

$$
f_{r}=s f_{e}=(0.06)(50 \mathrm{~Hz})=3.00 \mathrm{~Hz}
$$

## Problem 7-7 (pp.468-469)

A $208-\mathrm{V}$, two-pole, $60-\mathrm{Hz}$ Y-connected wound-rotor induction motor is rated at 15 hp . Its equivalent circuit components are

$$
\begin{array}{lll}
R_{1}=0.200 \Omega & R_{2}=0.120 \Omega & X_{M}=15.0 \Omega \\
X_{1}=0.410 \Omega & X_{2}=0.410 \Omega & \\
P_{\text {med }}=250 \mathrm{~W} & P_{\text {mixc }} \approx 0 & P_{\text {case }}=180 \mathrm{~W}
\end{array}
$$

For a slip of 0.05 , find
(a) The line current $I_{L}$
(b) The stator copper losses $P_{\text {SCL }}$
(c) The air-gap power $P_{A G}$
(d) The power converted from electrical to mechanical form $P_{\text {can }}$
(e) The induced torque $\tau_{\text {ind }}$
(f) The load torque $\tau_{\text {lasd }}$
(g) The overall machine efficiency
(h) The motor speed in revolutions per minute and radians per second

## Solution to Problem 7-7 (pp.468469)

Solumion The equivalent circuit of this induction motor is shown below:

(a) The easiest way to find the line current (or armature current) is to get the equivalent impedance $Z_{F}$ of the rotor circuit in parallel with $j X_{M}$, and then calculate the current as the phase voltage divided by the sum of the series impedances, as shown below.


The equivalent impedance of the rotor circuit in parallel with $j X_{M}$ is:

$$
Z_{F}=\frac{1}{\frac{1}{j X_{M}}+\frac{1}{Z_{2}}}=\frac{1}{\frac{1}{j 15 \Omega}+\frac{1}{2.40+j 0.41}}=2.220+j 0.745=2.34 \angle 18.5^{\circ} \Omega
$$

The phase voltage is $208 / \sqrt{3}=120 \mathrm{~V}$, so line current $I_{L}$ is

## Solution to Problem 7-7 (pp.468-469) Cont'd

$$
\begin{aligned}
& I_{L}=I_{A}=\frac{V_{\phi}}{R_{1}+j X_{1}+R_{F}+j X_{F}}=\frac{120 \angle 0^{\circ} \mathrm{V}}{0.20 \Omega+j 0.41 \Omega+2.22 \Omega+j 0.745 \Omega} \\
& I_{L}=I_{A}=44.8 \angle-25.5^{\circ} \mathrm{A}
\end{aligned}
$$

(b) The stator copper losses are

$$
P_{\mathrm{SCL}}=3 I_{A}{ }^{2} R_{1}=3(44.8 \mathrm{~A})^{2}(0.20 \Omega)=1205 \mathrm{~W}
$$

(c) The air gap power is $P_{A G}=3 I_{2}{ }^{2} \frac{R_{2}}{s}=3 I_{A}{ }^{2} R_{F}$
(Note that $3 I_{A}{ }^{2} R_{F}$ is equal to $3 I_{2}{ }^{2} \frac{R_{2}}{s}$, since the only resistance in the original rotor circuit was $R_{2} / s$, and the resistance in the Thevenin equivalent circuit is $R_{F}$. The power consumed by the Thevenin equivalent circuit must be the same as the power consumed by the original circuit.)

$$
P_{A G}=3 I_{2}{ }^{2} \frac{R_{2}}{s}=3 I_{A}{ }^{2} R_{F}=3(44.8 \mathrm{~A})^{2}(2.220 \Omega)=13.4 \mathrm{~kW}
$$

(d) The power converted from electrical to mechanical form is

$$
P_{\text {coav }}=(1-s) P_{\mathrm{AG}}=(1-0.05)(13.4 \mathrm{~kW})=12.73 \mathrm{~kW}
$$

(e) The induced torque in the motor is

$$
\tau_{\text {ind }}=\frac{P_{\mathrm{AG}}}{\omega_{\text {gnnc }}}=\frac{13.4 \mathrm{~kW}}{(3600 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \frac{1 \mathrm{~min}}{60 \mathrm{~s}}}=35.5 \mathrm{~N} \cdot \mathrm{~m}
$$

## Solution to Problem 7-7 (pp.468-469) Cont'd

(f) The output power of this motor is

$$
P_{\text {out }}=P_{\text {cocx }}-P_{\text {mech }}-P_{\text {cese }}-P_{\text {micc }}=12.73 \mathrm{~kW}-250 \mathrm{~W}-180 \mathrm{~W}-0 \mathrm{~W}=12.3 \mathrm{~kW}
$$

The output speed is

$$
n_{m}=(1-s) n_{\mathrm{gyx}}=(1-0.05)(3600 \mathrm{r} / \mathrm{min})=3420 \mathrm{r} / \mathrm{min}
$$

Therefore the load torque is

$$
\tau_{\text {load }}=\frac{P_{\mathrm{OUT}}}{\omega_{\mathrm{m}}}=\frac{12.3 \mathrm{~kW}}{(3420 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \quad \frac{1 \mathrm{~min}}{60 \mathrm{~s}}}=34.3 \mathrm{~N} \cdot \mathrm{~m}
$$

(g) The overall efficiency is

$$
\begin{aligned}
& \eta=\frac{P_{\mathrm{OUT}}}{P_{\mathrm{IN}}} \times 100 \%=\frac{P_{\mathrm{OUT}}}{3 V_{\phi} I_{A} \cos \theta} \times 100 \% \\
& \eta=\frac{12.3 \mathrm{~kW}}{3(120 \mathrm{~V})(44.8 \mathrm{~A}) \cos 25.5^{\circ}} \times 100 \%=84.5 \%
\end{aligned}
$$

(h) The motor speed in revolutions per minute is $3420 \mathrm{r} / \mathrm{min}$. The motor speed in radians per second is

$$
\omega_{\mathrm{m}}=(3420 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \quad \frac{1 \mathrm{~min}}{60 \mathrm{~s}}=358 \mathrm{rad} / \mathrm{s}
$$

## Problem 7-19 (p.470)

A $460-\mathrm{V}$, four-pole, $50-\mathrm{hp}, 60-\mathrm{Hz}$, Y-connected three-phase induction motor develops its full-load induced torque at 3.8 percent slip when operating at 60 Hz and 460 V . The per-phase circuit model impedances of the motor are

$$
\begin{array}{ll}
R_{1}=0.33 \Omega & X_{M}=30 \Omega \\
X_{1}=0.42 \Omega & X_{2}=0.42 \Omega
\end{array}
$$

Mechanical, core, and stray losses may be neglected in this problem.
(a) Find the value of the rotor resistance $R_{2}$.
(b) Find $\tau_{\max }, s_{\max }$, and the rotor speed at maximum torque for this motor.
(c) Find the starting torque of this motor.

## Solution to Problem 7-19 (pp.470)

Solumon The equivalent circuit for this motor is


The Thevenin equivalent of the input circuit is:

$$
Z_{\mathrm{TH}}=\frac{j X_{M}\left(R_{1}+j X_{1}\right)}{R_{1}+j\left(X_{1}+X_{M}\right)}=\frac{(j 30 \Omega)(0.33 \Omega+j 0.42 \Omega)}{0.33 \Omega+j(0.42 \Omega+30 \Omega)}=0.321+j 0.418 \Omega=0.527 \angle 52.5^{\circ} \Omega
$$

$$
\mathbf{V}_{\mathrm{TH}}=\frac{j X_{M}}{R_{1}+j\left(X_{1}+X_{M}\right)} \mathbf{V}_{\phi}=\frac{(j 30 \Omega)}{0.33 \Omega+j(0.42 \Omega+30 \Omega)}\left(265.6 \angle 0^{\circ} \mathrm{V}\right)=262 \angle 0.6^{\circ} \mathrm{V}
$$

## Solution to Problem 7-19 (pp.470) - Cont'd

(a) If losses are neglected, the induced torque in a motor is equal to its load torque. At full load, the output power of this motor is 50 hp and its slip is $3.8 \%$, so the induced torque is

$$
\begin{aligned}
& n_{m}=(1-0.038)(1800 \mathrm{r} / \mathrm{min})=1732 \mathrm{r} / \mathrm{min} \\
& \tau_{\text {ind }}=\tau_{\text {lood }}=\frac{(50 \mathrm{hp})(746 \mathrm{~W} / \mathrm{hp})}{(1732 \mathrm{r} / \mathrm{min}) \frac{2 \pi \mathrm{rad}}{1 \mathrm{r}} \frac{1 \mathrm{~min}}{60 \mathrm{~s}}}=205.7 \mathrm{~N} \cdot \mathrm{~m}
\end{aligned}
$$

The induced torque is given by the equation

$$
\tau_{\text {ind }}=\frac{3 V_{\mathrm{TH}}^{2} R_{2} / s}{\omega_{\text {pnc }}\left(R_{\mathrm{TH}}+R_{2} / s\right)^{2}+\left(X_{\mathrm{TH}}+X_{2}\right)^{2}}
$$

Substituting known values and solving for $R_{2} / s$ yields

$$
\begin{aligned}
& 205.7 \mathrm{~N} \cdot \mathrm{~m}=\frac{3(262 \mathrm{~V})^{2} R_{2} / s}{(188.5 \mathrm{rad} / \mathrm{s})\left(0.321+R_{2} / s\right)^{2}+(0.418+0.42)^{2}} \\
& 38,774=\frac{205,932 R_{2} / \mathrm{s}}{\left(0.321+R_{2} / s\right)^{2}+0.702} \\
& \left(0.321+R_{2} / s\right)^{2}+0.702=5.311 R_{2} / s \\
& 0.103+0.642 R_{2} / s+\left(R_{2} / s\right)^{2}+0.702=5.311 R_{2} / s
\end{aligned}
$$

## Solution to Problem 7-19 (pp.470) - Cont'd

$$
\begin{aligned}
& {\frac{R_{2}}{s}}^{2}-4.669 \frac{R_{2}}{s}+0.702=0 \\
& \frac{R_{2}}{s}=0.156,4.513
\end{aligned}
$$



$$
R_{2}=0.0059 \Omega, 0.172 \Omega
$$

These two solutions represent two situations in which the torque-speed curve would go through this specific torque-speed point. The two curves are plotted below. As you can see, only the $0.172 \Omega$ solution is realistic, since the $0.0059 \Omega$ solution passes through this torque-speed point at an unstable location on the back side of the torque-speed curve.

## Solution to Problem 7-19 (pp.470) - Cont'd

(b) The slip at pullout torque can be found by calculating the Thevenin equivalent of the input circuit from the rotor back to the power supply, and then using that with the rotor circuit model. The Thevenin equivalent of the input circuit was calculate in part (a). The slip at pullout torque is

$$
\begin{aligned}
& s_{\max }=\frac{R_{2}}{\sqrt{R_{\mathrm{TH}}^{2}+\left(X_{\mathrm{TH}}+X_{2}\right)^{2}}} \\
& s_{\max }=\frac{0.172 \Omega}{\sqrt{(0.321 \Omega)^{2}+(0.418 \Omega+0.420 \Omega)^{2}}}=0.192
\end{aligned}
$$

The rotor speed a maximum torque is

$$
n_{\text {pulkat }}=(1-s) n_{\text {syxx }}=(1-0.192)(1800 \mathrm{r} / \mathrm{min})=1454 \mathrm{r} / \mathrm{min}
$$

and the pullout torque of the motor is

$$
\begin{aligned}
& \tau_{\max }=\frac{3 V_{\mathrm{TH}}^{2}}{2 \omega_{\text {gix }} R_{\mathrm{TH}}+\sqrt{R_{\mathrm{TH}}^{2}+\left(X_{\mathrm{TH}}+X_{2}\right)^{2}}} \\
& \tau_{\max }=\frac{3(262 \mathrm{~V})^{2}}{2(188.5 \mathrm{rad} / \mathrm{s}) 0.321 \Omega+\sqrt{(0.321 \Omega)^{2}+(0.418 \Omega+0.420 \Omega)^{2}}} \\
& \tau_{\max }=448 \mathrm{~N} \cdot \mathrm{~m}
\end{aligned}
$$

(c) The starting torque of this motor is the torque at slip $s=1$. It is

$$
\begin{aligned}
& \tau_{\text {ind }}=\frac{3 V_{\mathrm{TH}}^{2} R_{2} / s}{\omega_{\mathrm{ync}}\left(R_{\mathrm{TH}}+R_{2} / s\right)^{2}+\left(X_{\mathrm{TH}}+X_{2}\right)^{2}} \\
& \tau_{\text {ind }}=\frac{3(262 \mathrm{~V})^{2}(0.172 \Omega)}{(188.5 \mathrm{rad} / \mathrm{s})(0.321+0.172 \Omega)^{2}+(0.418+0.420)^{2}}=199 \mathrm{~N} \cdot \mathrm{~m}
\end{aligned}
$$

# Transformers 

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## Transformer

An A.C. device used to change high voltage low current A.C. into low voltage high current A.C. and vice-versa without changing the frequency
In brief,

1. Transfers electric power from one circuit to another
2. It does so without a change of frequency 3. It accomplishes this by electromagnetic induction
3. Were the two electric circuits are in mutual ingon ine influence of each other.

## Principle of operation



## Constructional detail : Shell type



- Windings are wrapped around the center leg of a Iamsinated core.


## Core type



- Windings are wrapped around two sides of a laminated square core.


## Sectional view of transformers

(a)

(b)

(a) Shell-type transformer, (b) core-type transformer

Note:
High voltage conductors are smaller cross section conductors than the low voltage coils

## Construction of transformer from stampings

(a)

(b)

(a) Shell-type transformer, (b) core-type transformer

## Core type



Fig1: Coltadlaminations of core type transformo


## Shell type



- The HV and LV windings are split into no. of sections
- Where HV winding lies between two LV windings
- In sandwich coils leakage can be controlled

Fig: Sandwich windings

## Cut view of transformer



## Transformer with conservator and breather



## Working of a transformer

1. When current in the primary coil changes being alternating in nature, a changing magnetic field is produced
2. This changing magnetic field gets associated with the secondary through the soft iron core
3. Hence magnetic flux linked with the secondary coil changes.

4. Which induces e.m.f. in the secondary.

## Single Phase Transformer



FIGURE 4.8 A transformer circuit.

- A single phase transformer
- Two or more winding, coupled by a common magnetic core


## Ideal Transformers

- Zero leakage flux:
-Fluxes produced by the primary and secondary currents
are confined within the core
- The windings have no resistance:
- Induced voltages equal applied voltages
- The core has infinite permeability
- Reluctance of the core is zero
- Negligible current is required to establish magnetic flux
- Loss-less magnetic core
- No hysteresis or eddy currents


## Ideal transformer


$\mathrm{V}_{1}$ - supply voltage ;
$\mathrm{V}_{2-}$ output voltgae;
$\mathrm{I}_{\mathrm{m}}$ - magnetising current; $\mathrm{E}_{-}$-self induced emf;
$\mathrm{I}_{1}$ - noload input current ;
$\mathrm{I}_{2}$ - output current
$\mathrm{E}_{2}$ - mutually induced emf

## EMF equation of a transformer

- Worked out on board /
- Refer pdf file: emf-equation-of-tranformer


## Phasor diagram: Transformer on No-load


(a) Transformer on no-load (b) Phasor diagram of a transformer on no-load

## Transformer on load assuming no voltage drop in the winding



Fig shows the Phasor diagram of a transformer on load by assuming


1. No voltage drop in the winding
2. Equation of primary and secondary turns

## Transformer on load



Fig. a: Ideal transformer on load


Fig. b: Main flux and leakage flux in a transformer

## Phasor diagram of transformer with UPF Ioad



# Phasor diagram of transformer with lagging p.f load 



# Phasor diagram of transformer with leading p.f load 



## Equivalent circuit of a transformer

No load equivalent circuit:


$$
\begin{aligned}
& \mathrm{R}_{0}=\frac{\mathrm{V}_{1}}{\mathrm{I}_{\mathrm{c}}} \\
& \mathrm{X}_{0}=\frac{\mathrm{V}_{1}}{\mathrm{I}_{\mathrm{m}}}
\end{aligned}
$$

$\mathrm{I}_{\mathrm{m}}=\mathrm{I}_{0} \sin \phi_{0}=$ Magnetising component
$\mathrm{I}_{\mathrm{c}}=\mathrm{I}_{0} \cos \phi_{0}=$ Active component

## Equivalent circuit parameters referred to primary and secondary sides respectively



## Contd.,

- The effect of circuit parameters shouldn't be changed while transferring the parameters from one side to another side
- It can be proved that a resistance of $R_{2}$ in sec. is equivalent to $R_{2} / k^{2}$ will be denoted as $R_{2}$ '(ie. Equivalent sec. resistance w.r.t primary) which would have caused the same loss as $\mathrm{R}_{2}$ in secondary, $\quad I_{1}^{2} R_{2}=I_{2}^{2} R_{2}$

$$
\begin{aligned}
\mathrm{R}_{2}^{\prime} & =\left(\frac{I_{2}}{I_{1}}\right)^{2} R_{2} \\
& =\frac{\mathrm{R}_{2}}{\mathrm{k}^{2}}
\end{aligned}
$$

## Transferring secondary parameters to primary side

$$
\mathrm{R}_{2}^{\prime}=\frac{\mathrm{R}_{2}}{\mathrm{~K}^{2}}, \quad \mathrm{X}_{2}^{\prime}=\frac{\mathrm{X}_{2}}{\mathrm{~K}^{2}}, \quad \mathrm{Z}_{2}^{\prime}=\frac{\mathrm{Z}_{2}}{\mathrm{~K}^{2}}
$$

While

$$
\mathrm{E}_{2}^{\prime}=\frac{\mathrm{E}_{2}}{\mathrm{~K}^{\prime}} \quad \quad \mathrm{I}_{2}^{\prime}=\mathrm{KI}_{2}
$$

where

$$
\mathrm{K}=\frac{\mathrm{N}_{2}}{\mathrm{~N}_{1}}
$$



Exact equivalent circuit referred to primary

## Equivalent circuit referred to secondary side

-Transferring primary side parameters to secondary side

$$
\begin{array}{lll}
\mathrm{R}_{1}^{\prime}=\mathrm{K}^{2} \mathrm{R}_{1}, & \mathrm{X}_{1}^{\prime}=\mathrm{K}^{2} \mathrm{X}_{1}, & \mathrm{Z}_{1}^{\prime}=\mathrm{K}^{2} \mathrm{Z}_{1} \\
\mathrm{E}_{1}^{\prime}=\mathrm{K}_{1}, & \mathrm{I}_{1}^{\prime}=\frac{\mathrm{I}_{1}}{\mathrm{~K}^{\prime}} & \mathrm{I}_{0}^{\prime}=\frac{\mathrm{I}_{0}}{\mathrm{~K}}
\end{array}
$$

Similarly exciting circuit parameters are also transferred to secondary as $\mathrm{R}_{\mathrm{o}}{ }^{\prime}$ and $\mathrm{X}_{\mathrm{o}}{ }^{\prime}$


## equivalent circuit w.r.t primary


where

$$
\begin{aligned}
& \mathrm{R}_{01}=\mathrm{R}_{1}+\mathrm{R}_{2}^{\prime}=\mathrm{R}_{1}+\frac{\mathrm{R}_{2}}{\mathrm{~K}^{2}} \\
& \mathrm{X}_{01}=\mathrm{X}_{1}+\mathrm{X}_{2}^{\prime}=\mathrm{X}_{1}+\frac{\mathrm{X}_{2}}{\mathrm{~K}^{2}} \\
& \mathrm{Z}_{01}=\mathrm{R}_{01}+\mathrm{j} X_{01}
\end{aligned}
$$

## Approximate equivalent circuit

- Since the noload current is $1 \%$ of the full load current, the nolad circuit can be neglected



## Transformer Tests

-The performance of a transformer can be calculated on the basis of equivalent circuit
-The four main parameters of equivalent circuit are:

- $R_{01}$ as referred to primary (or secondary $R_{02}$ )
- the equivalent leakage reactance $X_{01}$ as referred to primary (or secondary $\mathrm{X}_{02}$ )
- Magnetising susceptance $B_{0}$ ( or reactance $X_{0}$ )
- core loss conductance $G_{0}$ (or resistance $R_{0}$ )
-The above constants can be easily determined by two tests
- Oper circuit test (O.C test / No load test)
- Short circuit test (S.C test/Impedance test)
-These tests are economical and convenient
- these tests furnish the result without actually loading the transformer


## Open-circuit Test

In Open Circuit Test the transformer's secondary winding is open-circuited, and its primary winding is connected to a full-rated line voltage.


$$
\begin{array}{rr}
\text { Core loss }=W_{o c}=V_{0} I_{0} \cos \phi_{0} & R_{0}=\frac{V_{0}}{I_{w}} \\
\cos \phi_{0}=\frac{W_{o c}}{V_{0} I_{0}} & X_{0}=\frac{V_{0}}{I \mu} \\
\mathrm{I}_{\mathrm{c}} \text { or } \mathrm{I}_{\mathrm{w}}=I_{0} \cos \phi_{0} & I
\end{array}
$$

- Usually conducted on H.V side
- To find
(i) No load loss or core loss
$\mathrm{W}_{\mathrm{oc}}=\mathrm{V}_{0}^{2} \mathrm{G}_{0} ; \therefore$ Exciting conductance $\mathrm{G}_{0}=\frac{\mathrm{W}_{\mathrm{oc}}}{\mathrm{V}_{0}^{2}}$
(ii) No load current $I_{0}$ which is helpful in finding $G_{0}\left(\right.$ or $\left.R_{0}\right)$ and $B_{0}$ (or $X_{0}$ )
\& Exciting susceptance $\mathrm{B}_{0}=\sqrt{Y_{0}^{2}-G_{0}^{2}}$


## Short-circuit Test

In Short Circuit Test the secondary terminals are short circuited, and the primary terminals are connected to a fairly low-voltage source
The input voltage is adjusted until the current in the short circuited windings is equal to its rated value. The input voltage, current and power is measured.


- Usually conducted on L.V side
- To find
(i) Full load copper loss - to pre determine the efficiency
(ii) $Z_{01}$ or $Z_{02} ; X_{01}$ or $X_{02} ; R_{01}$ or $R_{02}$ - to predetermine the voltage roulation


## Contd...



## Transformer Voltage Regulation and Efficiency

The output voltage of a transformer varies with the load even if the input voltage remains constant. This is because a real transformer has series impedance within it. Full load Voltage Regulation is a quantity that compares the output voltage at no load with the output voltage at full load, defined by this equation:

$$
\text { At noload } \mathrm{k}=\frac{\mathrm{V}_{\mathrm{s}}}{\mathrm{~V}_{\mathrm{p}}}
$$

Regulation up $=\frac{V_{S, n l}-V_{S, f l}}{V_{S, f l}} \times 100 \%$
Regulation up $=\frac{\left(V_{P} / k\right)-V_{S, f l}}{V_{S, f l}} \times 100 \%$
Regulation down $=\frac{V_{S, n}-V_{S, f}}{V_{S, n l}} \times 100 \%$
Regulation down $=\frac{\left(V_{P} / k\right)-V_{S, f l}}{V_{S, n l}} \times 100 \%$

Ideal transformer, $V R=0 \%$.

## Voltage regulation of a transformer

Voltage regulation $=\frac{\text { no }- \text { load voltage }- \text { full }- \text { load voltage }}{\text { no-load voltage }}$
recall $\frac{\mathrm{V}_{\mathrm{s}}}{\mathrm{V}_{\mathrm{p}}}=\frac{\mathrm{N}_{\mathrm{s}}}{\mathrm{N}_{\mathrm{p}}}$
Secondary voltage on no-load $\quad V_{2}=V_{1}\left(\frac{N_{2}}{N_{1}}\right)$
$\mathrm{V}_{2}$ is a secondary terminal voltage on full load

Substitute we have
Voltage regulation $=\frac{V_{1}\left(\frac{N_{2}}{N_{1}}\right)-V_{2}}{V_{1}\left(\frac{N_{2}}{N_{1}}\right)}$

## Transformer Phasor Diagram

To determine the voltage regulation of a transformer, it is necessary understand the voltage drops within it.

$$
\underbrace{2} \frac{R_{c}}{\mathrm{k}^{2}}
$$

## Transformer Phasor Diagram

Ignoring the excitation of the branch (since the current flow through the branch is considered to be small), more consideration is given to the series impedances ( $\mathrm{R}_{\mathrm{eq}}+\mathrm{j} \mathrm{X}_{\text {eq }}$ ).
Voltage Regulation depends on magnitude of the series impedance and the phase angle of the current flowing through the transformer.

Phasor diagrams will determine the effects of these factors on the voltage regulation. A phasor diagram consist of current and voltage vectors.

Assume that the reference phasor is the secondary voltage, $\mathrm{V}_{\mathrm{s}}$. Therefore the reference phasor will have 0 degrees in terms of angle.

Based upon the equivalent circuit, apply Kirchoff Voltage Law,

$$
\frac{V_{P}}{k}=V_{S}+R_{e q} I_{S}+j X_{e q} I_{S}
$$

## Transformer Phasor Diagram

For lagging loads, $V_{D} / a>V_{c}$ so the voltage regulation with lagging loads is $>0$.


When the power factor is unity, $V_{s}$ is lower than $V_{P}$ so VR $>0$.

(a)

## Transformer Phasor Diagram

With a leading power factor, $V_{s}$ is higher than the referred $V_{P}$ so $V R<0$

(b)

## Transformer Phasor Diagram

For lagging loads, the vertical components of $R_{\text {eq }}$ and $X_{\text {eq }}$ will partially cancel each other. Due to that, the angle of $\mathrm{V}_{\mathrm{p}} /$ a will be very small, hence we can assume that $\mathrm{V}_{\mathrm{p}} / \mathrm{k}$ is horizontal. Therefore the approximation will be as follows:


## Formula: voltage regulation

In terms of secondary values
$\%$ regulation $=\frac{{ }_{0} \mathrm{~V}_{2}-V_{2}}{{ }_{0} \mathrm{~V}_{2}}=\frac{I_{2} R_{02} \cos \phi_{2} \pm I_{2} X_{02} \sin \phi_{2}}{{ }_{0} \mathrm{~V}_{2}}$
where '+' for lagging and '-'for leading
In terms of primary values
$\%$ regulation $=\frac{\mathrm{V}_{1}-V_{2}^{\prime}}{\mathrm{V}_{1}}=\frac{I_{1} R_{01} \cos \phi_{1} \pm I_{1} X_{01} \sin \phi_{1}}{\mathrm{~V}_{1}}$
where '+' for lagging and '-'for leading

## Transformer Efficiency

Transformer efficiency is defined as (applies to motors, generators and transformers):

$$
\begin{aligned}
\eta & =\frac{P_{\text {out }}}{P_{\text {in }}} \times 100 \% \\
\eta & =\frac{P_{\text {out }}}{P_{\text {out }}+P_{\text {loss }}} \times 100 \%
\end{aligned}
$$

Types of losses incurred in a transformer:
Copper $I^{2}$ R losses
Hysteresis losses
Eddy current losses
Therefore, for a transformer, efficiency may be calculated using the following:

$$
\eta=\frac{V_{S} I_{S} \cos \theta}{P_{C u}+P_{\text {core }}+V_{S} I_{S} \cos \theta} \times 100 \%
$$

## Losses in a transformer

Core or Iron loss:
Hysteresis loss $\quad W_{h}=\eta B_{\text {max }}^{1.6} f V$ watt;
eddy current loss $W_{e}=\eta B_{\text {max }}^{2} f^{2} t^{2}$ watt

Copper loss:

$$
\text { Total Culoss }=I_{1}^{2} R_{1}+I_{2}^{2} R_{2}=I_{1}^{2} R_{01}+I_{2}^{2} R_{02}
$$

## Condition for maximum efficiency

$$
\begin{aligned}
\text { Cu loss } & =I_{1}{ }^{2} R_{01} \text { or } I_{2}{ }^{2} R_{02}=W_{c u} \\
\text { Iron loss } & =\text { Hysteresis loss }+ \text { Eddy current loss }=W_{h}+W_{e}=W_{i}
\end{aligned}
$$

Considering primary side,

$$
\begin{aligned}
\text { Primary input } & =V_{1} I_{1} \cos \phi_{1} \\
\eta & =\frac{V_{1} I_{1} \cos \phi_{1}-\operatorname{losses}}{V_{1} I_{1} \cos \phi_{1}}=\frac{V_{1} I_{1} \cos \phi_{1}-I_{1}^{2} R_{01}-W_{i}}{V_{1} I_{1} \cos \phi_{1}} \\
& =1-\frac{I_{1} R_{01}}{V_{1} \cos \phi_{1}}-\frac{W_{i}}{V_{1} I_{1} \cos \phi_{1}}
\end{aligned}
$$

Differentiating both sides with respect to $I_{1}$, we get

$$
\frac{d \eta}{d I_{1}}=0-\frac{R_{01}}{V_{1} \cos \phi_{1}}+\frac{W_{i}}{V_{1} I_{1}^{2} \cos \phi_{1}}
$$

For $\eta$ to be maximum, $\quad \frac{d \eta}{d I_{1}}=0$. Hence, the above equation becomes

$$
\frac{R_{01}}{V_{1} \cos \phi_{1}}=\frac{W_{i}}{V_{1} I_{1}^{2} \cos \phi_{1}} \text { or } W_{i}=I_{1}^{2} R_{01} \text { or } I_{2}^{2} R_{02}
$$

$$
\mathrm{Cu} \text { loss }=\text { Iron loss }
$$

## Contd.,

The output current corresponding to maximum efficiency is $I_{2}=\sqrt{\left(W_{i} / R_{02}\right)}$.

The load at which the two losses are equal =

$$
=\text { Full load } \times \sqrt{\left(\frac{\text { Iron loss }}{\text { FL Cu loss }}\right)}
$$

## All day efficiency

ordinary commercial efficiency $=\frac{\text { out put in watts }}{\text { input in watts }}$

$$
\left.\eta_{\text {all day }}=\frac{\text { output in } \mathrm{kWh}}{\text { Input in } \mathrm{kWh}} \text { (for } 24 \text { hours }\right)
$$

-All day efficiency is always less than the commercial efficiency

